

**SIDDHARTH INSTITUTE OF ENGINEERING & TECHNOLOGY:: PUTTUR**  
(AUTONOMOUS)  
**MCA I Year I Semester Regular Examinations December-2025**  
**MATHEMATICAL FOUNDATION OF COMPUTER SCIENCE**

**Time: 3 Hours**

(Answer all Five Units 5 x 12 = 60 Marks)

**Max. Marks: 60****UNIT-I**

- 1 a Explain the connectives and their truth tables. CO1 L1 6M  
b Prove that  $[(P \rightarrow Q) \wedge (Q \rightarrow R)] \rightarrow [P \rightarrow R]$  is a tautology. CO1 L3 6M

**OR**

- 2 a Define Predicates, simple and compound statement function with example. CO1 L1 6M  
b Prove that if  $n$  is an integer, then  $n^2 \geq n$ , by proof by cases method. CO1 L2 6M

**UNIT-II**

- 3 a Define (i) Equal sets (ii) Empty set (iii) Subset (iv) The size of a set CO2 L1 6M  
(v) Power set (vi) Cartesian Product of two sets  
b If  $f: R \rightarrow R$  such that  $f(x) = 2x+1$  and  $g: R \rightarrow R$  such that  $g(x) = \frac{x}{3}$  CO2 L2 6M  
then verify that  $(gof)^{-1} = f^{-1}og^{-1}$

**OR**

- 4 a Show that if  $A$  and  $B$  are countable sets, then  $A \cup B$  is also countable. CO2 L2 6M  
b Define transitive closures. Let  $A = \{1, 2, 3\}$  &  $R = \{(1, 2), (2, 3), (3, 1)\}$ . Find CO2 L2 6M  
the reflexive, symmetric and transitive closures of  $R$ , using composition of matrix relation of  $R$ .

**UNIT-III**

- 5 a Write the properties of algorithms. CO3 L1 6M  
b Define Big-O Notation with an example. CO3 L1 6M

**OR**

- 6 a Explain mathematical induction and strong induction CO3 L1 6M  
b Show that if  $n$  is an integer greater than 1, then  $n$  can be written as the CO3 L2 6M  
product of primes by using strong induction method

**UNIT-IV**

- 7 a A class consists of 6 girls and 10 boys. If a committee of 3 is chosen at random from the class, find the Probability that (i) 3 boys are selected CO4 L2 6M  
(ii) Exactly 2 girls are selected.  
b Two dice are thrown. Let  $A$  be the event that the sum of the point on the CO4 L2 6M  
faces is 9. Let  $B$  be the event that at least one number is 6. Find  
(i)  $P(A \cap B)$  (ii)  $P(A \cup B)$  (iii)  $P(A^c \cup B^c)$

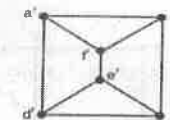
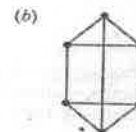
**OR**

- 8 A random variable  $X$  has the following probability function CO4 L2 12M

x	0	1	2	3	4	5	6	7
P(x)	0	k	2k	2k	3k	$k^2$	$2k^2$	$7k^2 + k$

Determine (i)  $k$  (ii)  $P(X \geq 6)$  and  $P(0 < x < 5)$ (iii) If  $P(X \leq k) > \frac{1}{2}$ , find the minimum value of  $k$  (iv) Variance**UNIT-V**

- 9 a How many vertices will the graph contains 6 edges and all vertices of CO5 L2 6M  
degree 3.  
b Explain about complete graph and Bipartite graph with an example CO5 L2 6M
- OR**
- 10 a Explain graph coloring and chromatic number give an example. CO5 L2 6M  
b Show that the two graphs shown below are isomorphic? CO5 L2 6M



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